

Lecture 5

Finite State Machines

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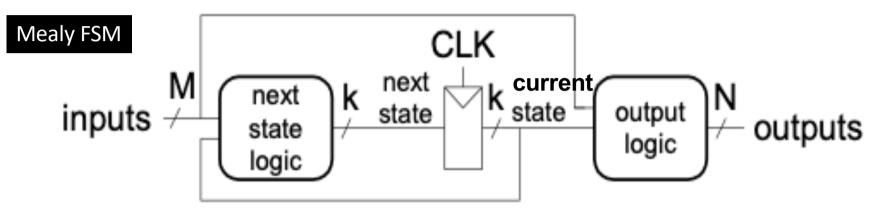
Lecture 5 Slide 1

Lecture Objectives

- To learn how to **analyse** a state machine
- To learn how to **design** a state machine to meet specific objectives
- Learn how to specify a FSM in SystemVerilog
- How to combine a FSM with a counter to control state transition

Synchronous State Machines

Synchronous State Machine (also called Finite State Machine FSM)

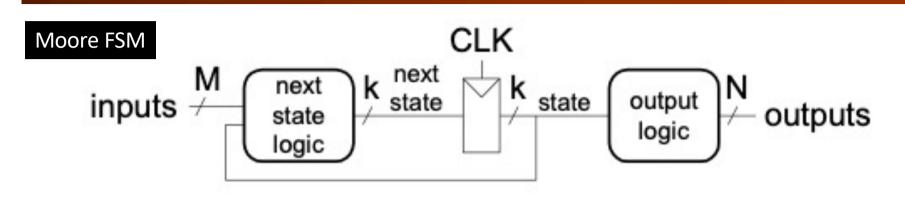


- The *current state* is defined by the register contents
- Register has k flipflops $\Rightarrow 2^k$ possible states
- The state only ever changes on CLOCK[↑]
 - We stay in a state for an exact number of CLOCK cycles
- The state is the only memory of the past
- Output can depend on both current state and current input Mealy FSM

<u>Rules:</u>

- Never mess around with the clock signal
- Always initialise the FSM to a known initial state on reset or power ON.

Simple FSM – Moore FSM

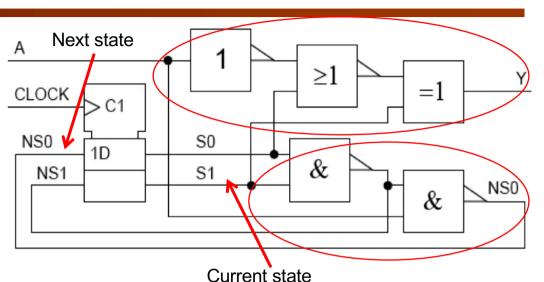


- Three parts:
 - *** State registers**
 - Next state logic
 - Output logic
- **Moore FSM** special case of Mealy FSM, output depends only on current state

Analysing a State Machine

State Table:

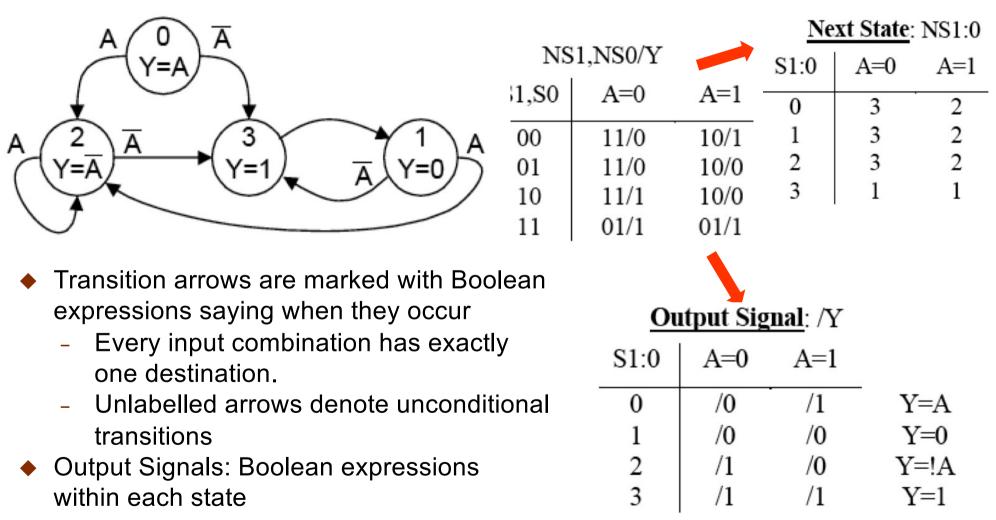
- Truth table for the combinational logic:
- One row per state: *n* flipflops $\Rightarrow 2^n$ rows
- One column per input combination: *m* input signals $\Rightarrow 2^m$ columns
- Each cell specifies the *next state* and the *output signals during the current state*
 - for clarity, we separate the two using a /



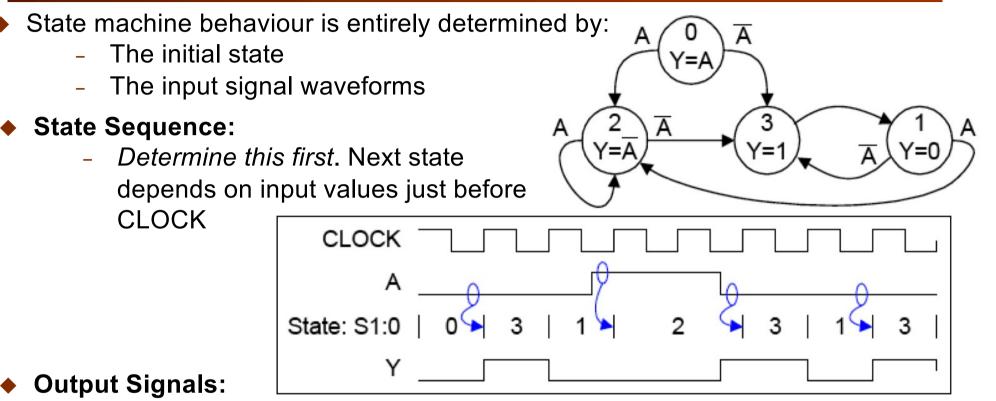
NS1,NS0/Y S1,S0 A=0A=111/010/100 11/001 10/011/110 10/011 01/101/1

Drawing the State Diagram

• Split state table into two parts: next state table and output table



Timing Diagram



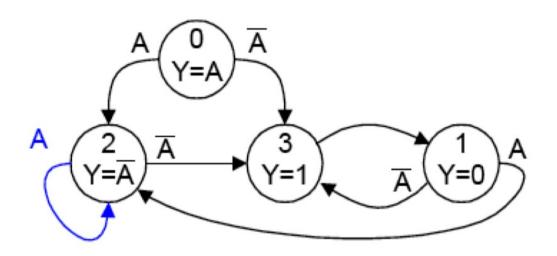
Defined by Boolean expressions within each state.

If all the expressions are constant 0 or 1 then outputs only ever change on clock . (*Moore machine*)

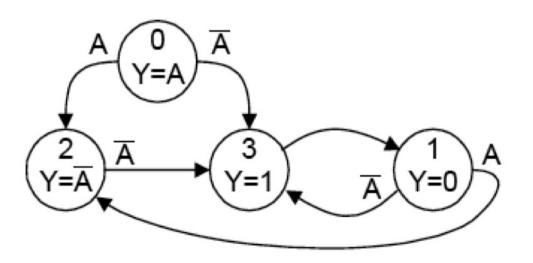
If any expressions involve the inputs (e.g. Y=A) then it is possible for the outputs to change in the middle of a state. (*Mealy machine*)

Self-Transitions

- We can omit transitions from a state to itself
 - Aim: to save clutter on the diagram

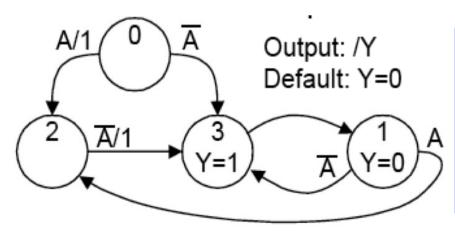


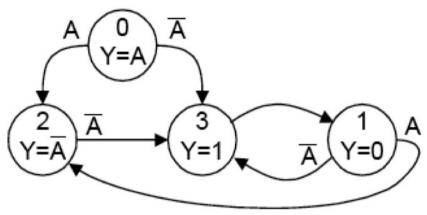
- The state machine remains in its current state if none of the transition-arrow conditions are satisfied
 - From state 2, we go to state 3 if !A occurs, otherwise we remain in state 2



Output Expressions on Arrows

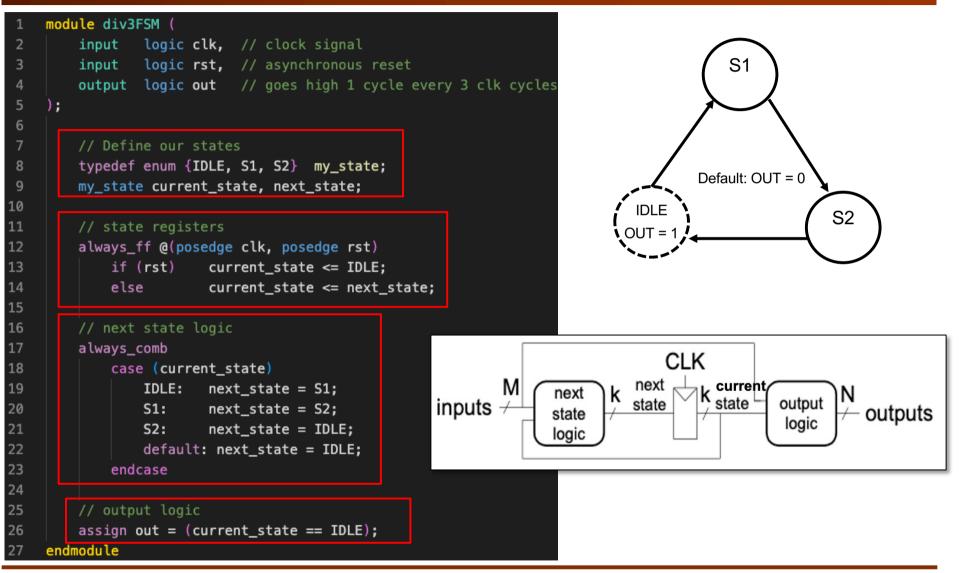
- It may make the diagram clearer to put output expressions on the arrows instead of within the state circles:
 - Useful if the same Boolean expression determines both the *next state* and the *output signals*
 - For each state, the output specification must be *either* inside the circle *or else* on *every* emitted arrow
 - If self transitions are omitted, we must declare default values for the outputs





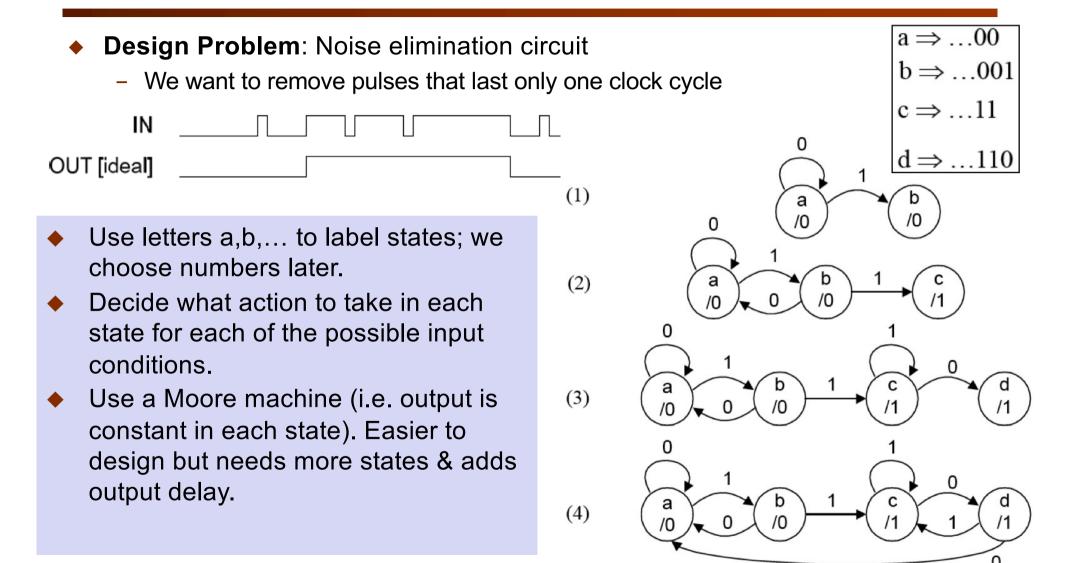
- Outputs written on an arrow apply to the state emitting the arrow.
- Outputs still apply for the entire time spent in a state
- This does not affect the Moore/Mealy distinction
- This is a notation change only

Example 1: Divide by 3 FSM (Moore)



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Example 2: Design a Noise Pulse Eliminator (1)



Design a Noise Pulse Eliminator (2)

- 1. If IN goes high for two (or more) clock cycles then OUT must go high, whereas if it goes high for only one clock cycle then OUT stays low. It follows that the two histories "IN low for ages" and "IN low for ages then high for one clock" are different because if IN is high for the next clock we need different outputs. Hence we need to introduce state b.
- 2. If IN goes high for one clock and then goes low again, we can forget it ever changed at all. This glitch on IN will not affect any of our future actions and so we can just return to state a.

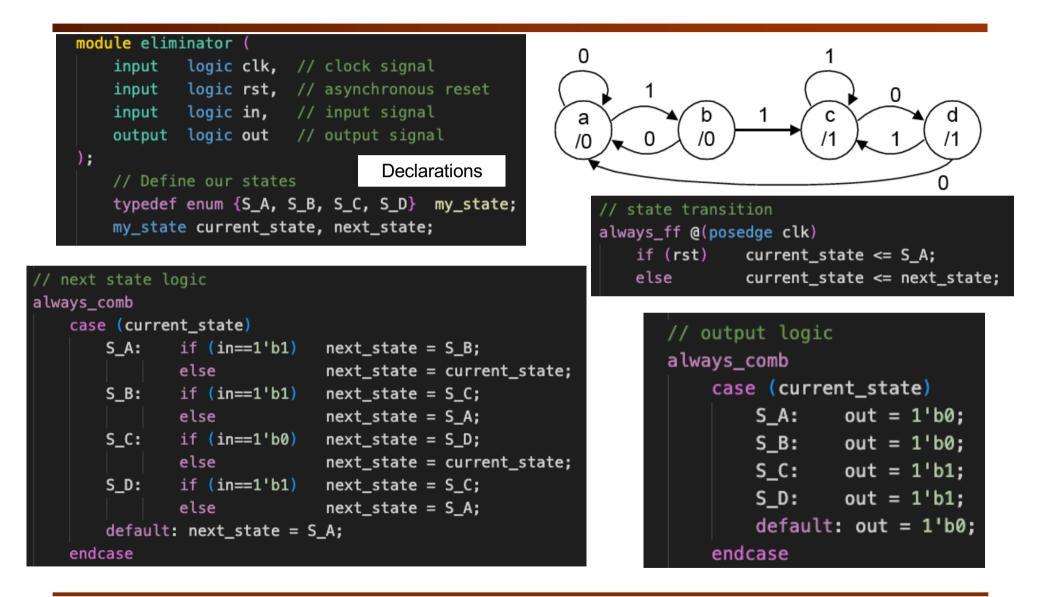
If on the other hand we are in state b and IN stays high for a second clock cycle, then the output must change. It follows that we need a new state, c.

- 3. The need for state d is exactly the same as for state b earlier. We reach state d at the end of an output pulse when IN has returned low for one clock cycle. We don't change OUT yet because it might be a false alarm.
- 4. If we are in state d and IN remains low for a second clock cycle, then it really is the end of the pulse and OUT must go low. We can forget the pulse ever existed and just return to state a.

Each state represents a particular history that we need to distinguish from the others:

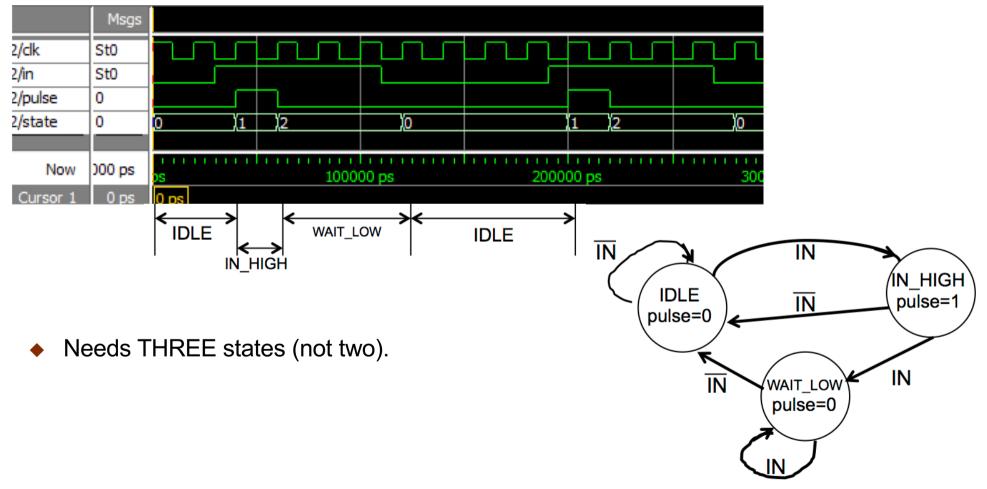
state **a**: IN=0 for >1 clock state **c**: IN=1 for >1 clock state **b**: IN=1 for 1 clock state **d**: IN=0 for 1 clock

Eliminator design in SystemVerilog



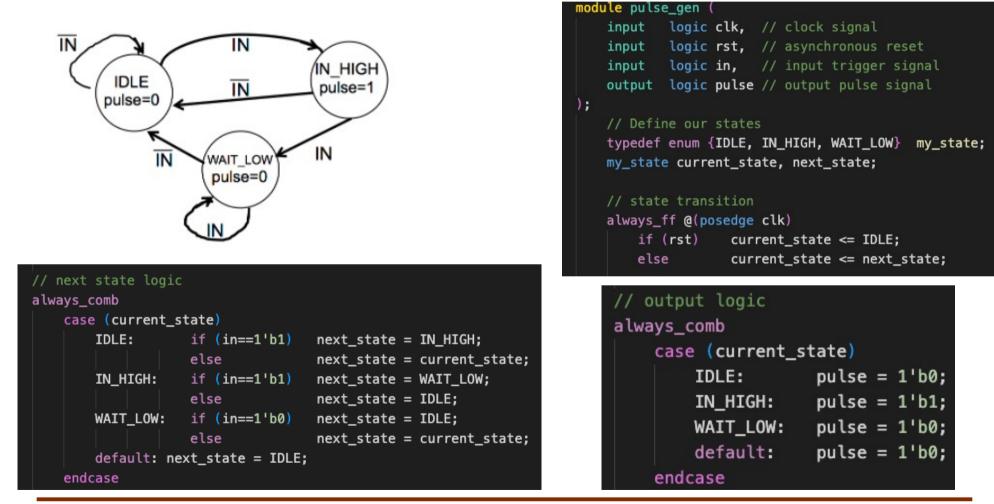
Example 3 – A pulse generator

 Design a module pulse_gen.v which does the following: on each positive edge of the input signal IN, it generates a pulse lasting for one period of the input clock.



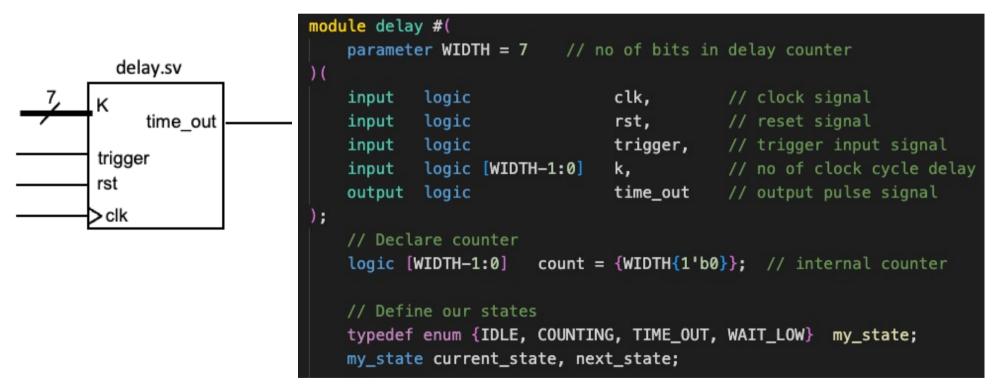
Pulse Generator in SystemVerilog

 Design a module pulse_gen.v which does the following: on each positive edge of the input signal IN, it generates a pulse lasting for one period of the input clk.

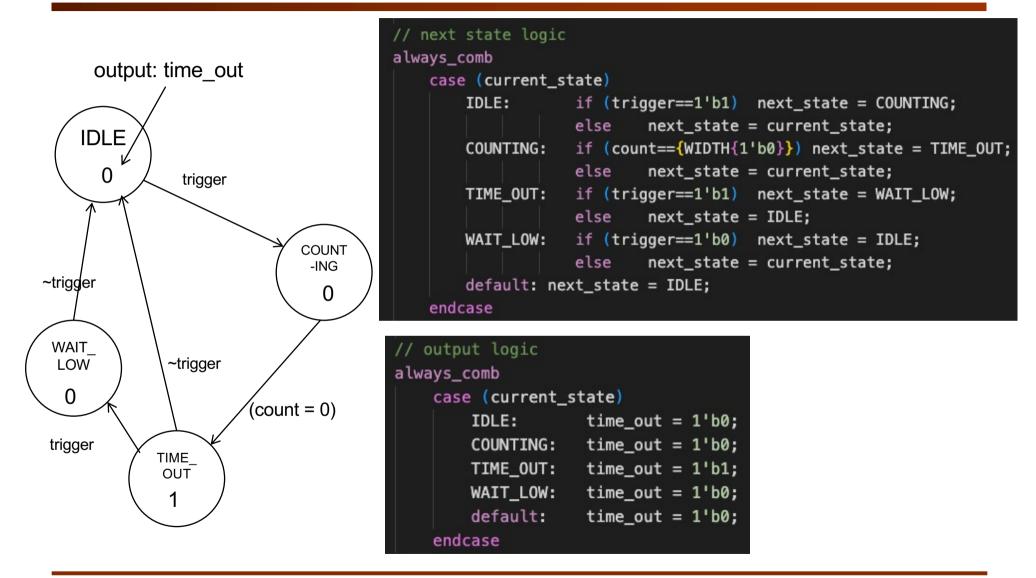


Example 4: delay module (1)

- Here is a very useful module that combines a FSM with a counter.
- It detects the rising edge on trigger, then wait (delay) for n clk cycles before producing a 1-cycle pulse on time_out.
- The external port interface for this module is shown below. We assume that n is a 7-bit number, or a maximum of 127 sysclk cycles delay.



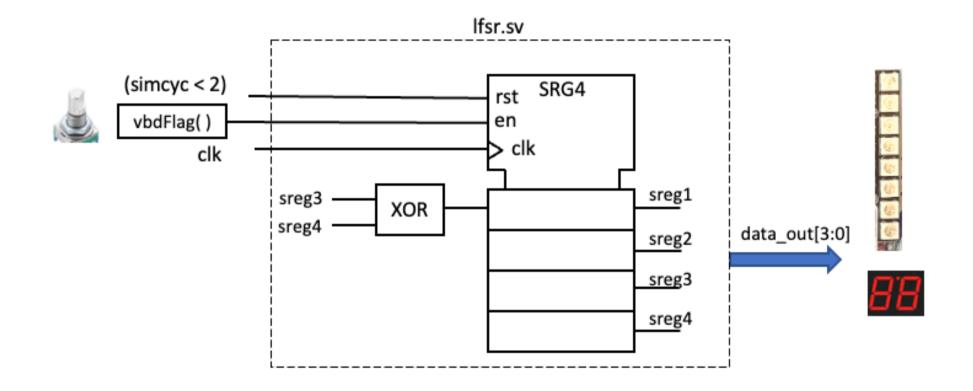
Example 4: delay module (2)



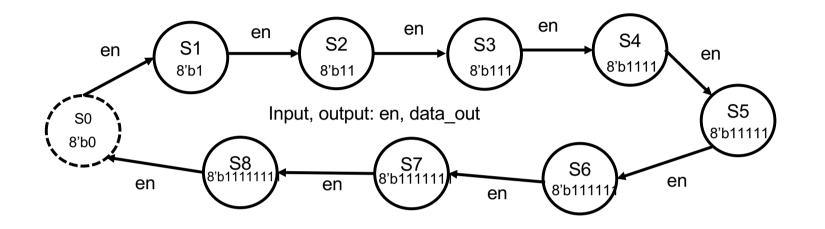
Example 4: delay module (3)

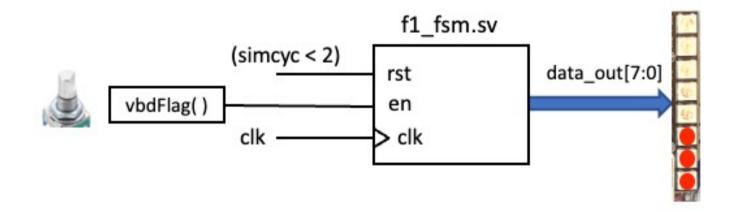


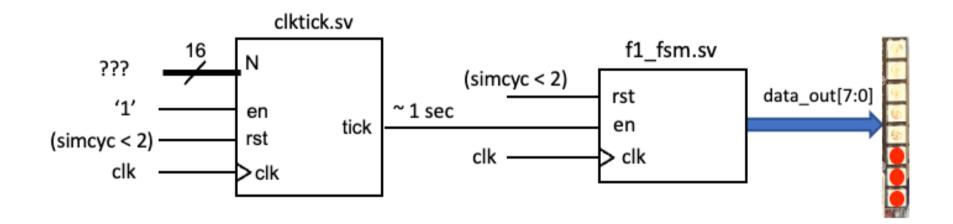
Lab 3 Task 1 – LFSR and random number generator



Lab 3 Task 2 – FSM & F1 light sequence







Lab 3 Task 4 – F1 starting light (optional)

